

TMUA Practice - Trigonometry

1. What is the largest solution for x in the range $0 \leq x < 2\pi$ for the following equation:

$$2\sin\left(2x - \frac{\pi}{3}\right) + 1 = 0$$

- A $\frac{\pi}{12}$ B $\frac{3\pi}{4}$ C $\frac{13\pi}{12}$ D $\frac{7\pi}{4}$ E $\frac{23\pi}{12}$

2. What is the sum of the solutions for x in the range $0 \leq x < \pi$ for the following equation:

$$\tan(2x - \pi) = 1$$

- A $\frac{\pi}{8}$ B $\frac{5\pi}{8}$ C $\frac{3\pi}{4}$ D $\frac{5\pi}{4}$ E $\frac{7\pi}{4}$

3. How many solutions does the following equation have in the range $0 \leq x < 2\pi$

$$2\sin(\cos x) = \sqrt{2}$$

- A 0
B 1
C 2
D 3
E infinitely many

4. x satisfies the simultaneous equations

$$2\sqrt{2}\sin 3x - \tan 3x = 3$$

$$\sqrt{2}\tan 3x + 4\sin 3x = \sqrt{2}$$

where $0 \leq x \leq 180$.

Find the sum of the possible values of x

- A 150
- B 210
- C 315
- D 360
- E 540

5. Consider the inequality

$$\sin\left(x + \frac{\pi}{3}\right) \geq \frac{1}{2}$$

The fraction of the interval $0 \leq x \leq 2\pi$ for which this is true, is:

- A $\frac{1}{6}$
- B $\frac{1}{4}$
- C $\frac{1}{3}$
- D $\frac{5}{12}$
- E $\frac{1}{2}$

6. Find the greatest value of the function $f(x) = (3\sin^2(2x - 5) - 7)^2$

- A 16
- B 25
- C 36
- D 49
- E 100

7. Find the maximum value of $3(4^{\sin x}) - 10(2^{\sin x}) + 9$

- A $\frac{2}{3}$ B 1 C 2 D $\frac{19}{4}$ E 9

8. Which of the following is the largest?

- A $\tan\left(\frac{5\pi}{4}\right)$ B $\sin^2\left(\frac{3\pi}{4}\right)$ C $\log_{10}\left(\frac{5\pi}{4}\right)$ D $\log_2\left(\frac{3\pi}{4}\right)$

9. A triangle ABC is drawn with $AC = 5\text{cm}$ and $BC = 11\text{cm}$ and the angle at B equal to a specified angle θ .

Of the two possible triangles that could be drawn, the larger triangle has double the area of the smaller one.

What is the value of $\cos\theta$?

- A $\frac{10}{11}$ B $\frac{3\sqrt{12}}{11}$ C $\frac{\sqrt{13}}{11}$ D $\frac{\sqrt{6}}{5}$ E $\frac{3\sqrt{6}}{25}$

10. A triangle ABC is to be drawn with the following measurements.

$AB = 10\text{cm}$ and angle $BAC = 60^\circ$.

Which of the following statements is/are true ?

- I No such triangle can be drawn if $BC = 7\text{cm}$
 - II Exactly one distinct triangle can be drawn if $BC = 5\sqrt{3}\text{cm}$
 - III Exactly two distinct triangles can be drawn if $BC = 12\text{cm}$
- A none of them
 - B I only
 - C II only
 - D III only
 - E I and II only
 - F II and III only
 - G I and III only
 - H I, II and III